

**RD SHARMA**

**Solutions**

**Class 7 Maths**

**Chapter 23**

**Ex 23.2**

**Q1) A die was thrown 20 times and the following scores were recorded:**

**5, 2, 1, 3, 4, 4, 5, 6, 2, 2, 4, 5, 5, 6, 2, 2, 4, 5, 5, 1**

**Prepare the frequency table of the scores on the upper face of the die and find the mean score.**

**Solution:**

The frequency table for the given data is as follows:

x:    1    2    3    4    5    6  
f:    2    5    1    4    6    2

In order to compute the arithmetic mean, we prepare the following table:

**Computation of Arithmetic Mean**

| Scores ( $x_i$ ) | Frequency ( $f_i$ ) | $x_i f_i$           |
|------------------|---------------------|---------------------|
| 1                | 2                   | 2                   |
| 2                | 5                   | 10                  |
| 3                | 1                   | 3                   |
| 4                | 4                   | 16                  |
| 5                | 6                   | 30                  |
| 6                | 2                   | 12                  |
| Total            | $\sum f_i = 20$     | $\sum f_i x_i = 73$ |

We have,  $\sum f_i = 20$  and  $\sum f_i x_i = 73$

$$\therefore \text{Mean score} = \frac{\sum f_i x_i}{\sum f_i} = \frac{73}{20} = 3.65.$$

**Q2) The daily wages (in Rs) of 15 workers in a factory are given below:**

**200, 180, 150, 150, 130, 180, 180, 200, 150, 130, 180, 180, 200, 150, 180**

**Prepare the frequency table and find the mean wage.**

**Solution:**

The frequency table for the given data is as follows:

Wages ( $x_i$ ):            130   150   180   200  
Number of workers ( $f_i$ ):    2    4    6    3

In order to compute the mean wage, we prepare the following table:

**Mean wages of the workers**

| $x_i$ | $f_i$ | $x_i f_i$ |
|-------|-------|-----------|
| 130   | 2     | 260       |
| 150   | 4     | 600       |
| 180   | 6     | 1080      |
|       |       |           |

|       |                     |                       |
|-------|---------------------|-----------------------|
| 200   | 3                   | 600                   |
| Total | $\sum f_i = N = 15$ | $\sum f_i x_i = 2540$ |

$$\therefore \text{Mean} = \frac{\sum f_i x_i}{\sum f_i} = \frac{2540}{15} = 169.33.$$

**Q3) The following table shows the weights (in kg) of 15 workers in a factory:**

|                            |           |           |           |           |           |
|----------------------------|-----------|-----------|-----------|-----------|-----------|
| <b>Weight (in kg):</b>     | <b>60</b> | <b>63</b> | <b>66</b> | <b>72</b> | <b>75</b> |
| <b>Numbers of workers:</b> | <b>4</b>  | <b>5</b>  | <b>3</b>  | <b>1</b>  | <b>2</b>  |

**Calculate the mean weight.**

**Solution:**

**Calculation of Mean**

| $X_i$ | $f_i$           | $x_i f_i$            |
|-------|-----------------|----------------------|
| 60    | 4               | 240                  |
| 63    | 5               | 315                  |
| 66    | 3               | 198                  |
| 72    | 1               | 72                   |
| 75    | 2               | 150                  |
| Total | $\sum f_i = 15$ | $\sum f_i x_i = 975$ |

$$\therefore \text{Mean Weight} = \frac{\sum f_i x_i}{\sum f_i} = \frac{975}{15} = 65 \text{ kg.}$$

**Q4) The ages (in years) of 50 students of a class in a school are given below:**

|                             |           |           |           |           |           |
|-----------------------------|-----------|-----------|-----------|-----------|-----------|
| <b>Age (in years):</b>      | <b>14</b> | <b>15</b> | <b>16</b> | <b>17</b> | <b>18</b> |
| <b>Numbers of students:</b> | <b>15</b> | <b>14</b> | <b>10</b> | <b>8</b>  | <b>3</b>  |

**Find the mean age.**

**Solution:**

**Calculation of Mean**

| $X_i$ | $f_i$ | $x_i f_i$ |
|-------|-------|-----------|
| 14    | 15    | 210       |
| 15    | 14    | 210       |
| 16    | 10    | 160       |
| 17    | 8     | 136       |
| 18    | 3     | 54        |
|       |       |           |

|       |                 |                      |
|-------|-----------------|----------------------|
| Total | $\sum f_i = 50$ | $\sum f_i x_i = 770$ |
|-------|-----------------|----------------------|

$$\therefore \text{Mean Weight} = \frac{\sum f_i x_i}{\sum f_i} = \frac{770}{50} = 15.4 \text{ yrs.}$$

**Q5) Calculate the mean for the following distribution:**

|           |   |   |    |    |   |
|-----------|---|---|----|----|---|
| <b>x:</b> | 5 | 6 | 7  | 8  | 9 |
| <b>f:</b> | 4 | 8 | 14 | 11 | 3 |

**Solution:**

**Calculation of Mean**

| $X_i$ | $f_i$           | $x_i f_i$            |
|-------|-----------------|----------------------|
| 5     | 4               | 20                   |
| 6     | 8               | 48                   |
| 7     | 14              | 98                   |
| 8     | 11              | 88                   |
| 9     | 3               | 27                   |
| Total | $\sum f_i = 40$ | $\sum f_i x_i = 281$ |

$$\therefore \text{Mean} = \frac{\sum f_i x_i}{\sum f_i} = \frac{281}{40} = 7.025.$$

**Q6) Find the mean of the following data:**

|           |    |    |    |    |    |    |    |
|-----------|----|----|----|----|----|----|----|
| <b>x:</b> | 19 | 21 | 23 | 25 | 27 | 29 | 31 |
| <b>f:</b> | 13 | 15 | 16 | 18 | 16 | 15 | 13 |

**Solution:**

**Calculation of Mean**

| $X_i$ | $f_i$                | $x_i f_i$             |
|-------|----------------------|-----------------------|
| 19    | 13                   | 247                   |
| 21    | 15                   | 315                   |
| 23    | 16                   | 368                   |
| 25    | 18                   | 450                   |
| 27    | 16                   | 432                   |
| 29    | 15                   | 435                   |
| 31    | 13                   | 403                   |
| Total | $\sum f_i = N = 106$ | $\sum f_i x_i = 2650$ |

$$\therefore \text{Mean} = \frac{\sum f_i x_i}{\sum f_i} = \frac{2650}{106} = 25.$$

*Q7) The mean of the following data is 20.6. Find the value of p.*

|            |    |    |          |    |    |
|------------|----|----|----------|----|----|
| <i>x</i> : | 10 | 15 | <i>p</i> | 25 | 35 |
| <i>f</i> : | 3  | 10 | 25       | 7  | 5  |

**Solution:**

**Calculation of Mean**

| $X_i$    | $f_i$           | $x_i f_i$                  |
|----------|-----------------|----------------------------|
| 10       | 3               | 30                         |
| 15       | 10              | 150                        |
| <i>p</i> | 25              | 25 <i>p</i>                |
| 25       | 7               | 175                        |
| 35       | 5               | 175                        |
| Total    | $\sum f_i = 50$ | $\sum f_i x_i = 530 + 25p$ |

We have:

$$\therefore \text{Mean} = \frac{\sum f_i x_i}{\sum f_i}$$

$$\Rightarrow 20.6 = \frac{530 + 25p}{50}$$

$$\Rightarrow 530 + 25p = 20.6 \times 50$$

$$\Rightarrow 25p = 1030 - 530$$

$$\Rightarrow p = \frac{500}{25}$$

$$\Rightarrow p = 20$$

*Q8) If the mean of the following data is 15, find p.*

|            |   |          |    |    |    |
|------------|---|----------|----|----|----|
| <i>x</i> : | 5 | 10       | 15 | 20 | 25 |
| <i>f</i> : | 6 | <i>p</i> | 6  | 10 | 5  |

**Solution:**

**Calculation of Mean**

| $X_i$ | $f_i$    | $x_i f_i$   |
|-------|----------|-------------|
| 5     | 6        | 30          |
| 10    | <i>p</i> | 10 <i>p</i> |
| 15    | 6        | 90          |
| 20    | 10       | 200         |
| 25    | 5        | 125         |

|       |                     |                            |
|-------|---------------------|----------------------------|
| Total | $\sum f_i = 27 + p$ | $\sum f_i x_i = 445 + 10p$ |
|-------|---------------------|----------------------------|

We have:

$$\sum f_i = 27 + p, \sum f_i x_i = 445 + 10p$$

$$\therefore \text{Mean} = \frac{\sum f_i x_i}{\sum f_i}$$

$$\Rightarrow 15 = \frac{445 + 10p}{27 + p}$$

$$\Rightarrow 445 + 10p = 405 + 15p$$

$$\Rightarrow 5p = 445 - 405$$

$$\Rightarrow p = \frac{40}{5}$$

$$\Rightarrow p = 8.$$

**Q9) Find the value of p for the following distribution whose mean is 16.6**

**x:**    8    12    15    p    20    25    30

**f:**    12    16    20    24    16    8    4

**Solution:**

**Calculation of Mean**

| $X_i$ | $f_i$                | $X_i f_i$                   |
|-------|----------------------|-----------------------------|
| 8     | 12                   | 96                          |
| 12    | 16                   | 192                         |
| 15    | 20                   | 300                         |
| p     | 24                   | 24p                         |
| 20    | 16                   | 320                         |
| 25    | 8                    | 200                         |
| 30    | 4                    | 120                         |
| Total | $\sum f_i = N = 100$ | $\sum f_i x_i = 1228 + 24p$ |

We have:

$$\sum f_i = 100, \sum f_i x_i = 1228 + 24p$$

$$\therefore \text{Mean} = \frac{\sum f_i x_i}{\sum f_i}$$

$$\Rightarrow 16.6 = \frac{1228 + 24p}{100}$$

$$\Rightarrow 1228 + 24p = 16.6 \times 100$$

$$\Rightarrow 24p = 1660 - 1228$$

$$\Rightarrow p = \frac{432}{24}$$

$$\Rightarrow p = 18.$$

Q10) Find the missing value of  $p$  for the following distribution whose mean is 12.58

|      |   |   |    |    |     |    |    |
|------|---|---|----|----|-----|----|----|
| $x:$ | 5 | 8 | 10 | 12 | $p$ | 20 | 25 |
| $f:$ | 2 | 5 | 8  | 22 | 7   | 4  | 2  |

**Solution:**

**Calculation of Mean**

| $X_i$ | $f_i$               | $X_i f_i$                 |
|-------|---------------------|---------------------------|
| 5     | 2                   | 10                        |
| 8     | 5                   | 40                        |
| 10    | 8                   | 80                        |
| 12    | 22                  | 264                       |
| $p$   | 7                   | $7p$                      |
| 20    | 4                   | 80                        |
| 25    | 2                   | 50                        |
| Total | $\sum f_i = N = 50$ | $\sum f_i X_i = 524 + 7p$ |

We have:

$$\sum f_i = 50, \sum f_i X_i = 524 + 7p$$

$$\therefore \text{Mean} = \frac{\sum f_i X_i}{\sum f_i}$$

$$\Rightarrow 12.58 = \frac{524 + 7p}{50}$$

$$\Rightarrow 524 + 7p = 12.58 \times 50$$

$$\Rightarrow 7p = 629 - 524$$

$$\Rightarrow p = \frac{105}{7}$$

$$\Rightarrow p = 15.$$

Q11) Find the missing frequency ( $p$ ) for the following distribution whose mean is 7.68

|      |   |   |    |     |    |    |
|------|---|---|----|-----|----|----|
| $x:$ | 3 | 5 | 7  | 9   | 11 | 13 |
| $f:$ | 6 | 8 | 15 | $p$ | 8  | 4  |

**Solution:**

**Calculation of Mean**

| $X_i$ | $f_i$ | $X_i f_i$ |
|-------|-------|-----------|
| 3     | 6     | 10        |
| 5     | 8     | 40        |
| 7     | 15    | 80        |

|       |                     |                           |
|-------|---------------------|---------------------------|
| 9     | p                   | 264                       |
| 11    | 8                   | 7p                        |
| 13    | 4                   | 80                        |
| Total | $\sum f_i = 41 + p$ | $\sum f_i x_i = 303 + 9p$ |

We have:

$$\sum f_i = 41 + p, \sum f_i x_i = 303 + 9p$$

$$\therefore \text{Mean} = \frac{\sum f_i x_i}{\sum f_i}$$

$$\Rightarrow 7.68 = \frac{303+9p}{41+p}$$

$$\Rightarrow 303 + 9p = 314.88 + 7.68p$$

$$\Rightarrow 1.32p = 314.88 - 303$$

$$\Rightarrow p = \frac{11.88}{1.32}$$

$$\Rightarrow p = 9.$$

**Q12) Find the value of p, if the mean of the following distribution is 20**

|            |    |    |    |      |    |
|------------|----|----|----|------|----|
| <i>x</i> : | 15 | 17 | 19 | 20+p | 23 |
| <i>f</i> : | 2  | 3  | 4  | 5p   | 6  |

**Solution:**

**Calculation of Mean**

| $X_i$  | $f_i$                | $x_i f_i$                        |
|--------|----------------------|----------------------------------|
| 15     | 2                    | 30                               |
| 17     | 3                    | 51                               |
| 19     | 4                    | 76                               |
| 20 + p | 5p                   | (20 + p) 5p                      |
| 23     | 6                    | 138                              |
| Total  | $\sum f_i = 15 + 5p$ | $\sum f_i x_i = 295 + (20+p) 5p$ |

We have:

$$\sum f_i = 15 + 5p, \sum f_i x_i = 295 + (20+p) 5p$$

$$\therefore \text{Mean} = \frac{\sum f_i x_i}{\sum f_i}$$

$$\Rightarrow 20 = \frac{(295+(20+p)5p)}{15+5p}$$

$$\Rightarrow 295 + 100p + 5p^2 = 300 + 100p$$

$$\Rightarrow 5p^2 = 300 - 295$$



$$\Rightarrow 5p^2 = 5$$

$$\Rightarrow p^2 = 1$$

$$\Rightarrow p = 1.$$