

RD SHARMA

Solutions

Class 9 Maths

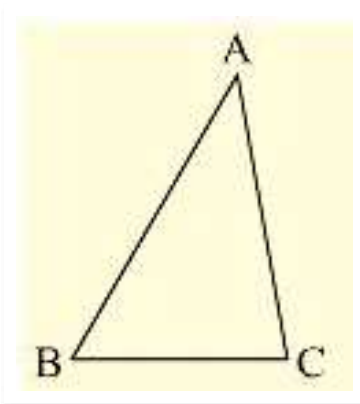
Chapter 10

Ex 10.6

(1) In $\triangle ABC$, if $\angle A = 40^\circ$ and $\angle B = 60^\circ$. Determine the longest and shortest sides of the triangle.

Solution:

Given that in $\triangle ABC$, $\angle A = 40^\circ$ and $\angle B = 60^\circ$



We have to find longest and shortest side

We know that,

Sum of angles in a triangle 180°

$$\angle A + \angle B + \angle C = 180^\circ$$

$$40^\circ + 60^\circ + \angle C = 180^\circ$$

$$\angle C = 180^\circ - (100^\circ) = 80^\circ$$

$$\angle C = 80^\circ$$

Now,

$$\Rightarrow 40^\circ < 60^\circ < 80^\circ = \angle A < \angle B < \angle C$$

$\Rightarrow \angle C$ is greater angle and $\angle A$ is smaller angle.

Now, $\angle A < \angle B < \angle C$

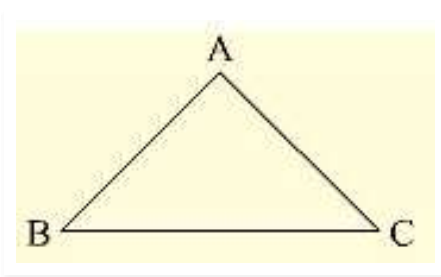
$\Rightarrow BC < AC < AB$ [Side opposite to greater angle is larger and side opposite to smaller angle is smaller]

AB is longest and BC is smallest or shortest side.

(2) In a $\triangle ABC$, if $\angle B = \angle C = 45^\circ$, which is the longest side?

Solution: Given that in $\triangle ABC$,

$$\angle B = \angle C = 45^\circ$$



We have to find longest side

We know that.

Sum of angles in a triangle = 180°

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle A + 45^\circ + 45^\circ = 180^\circ$$

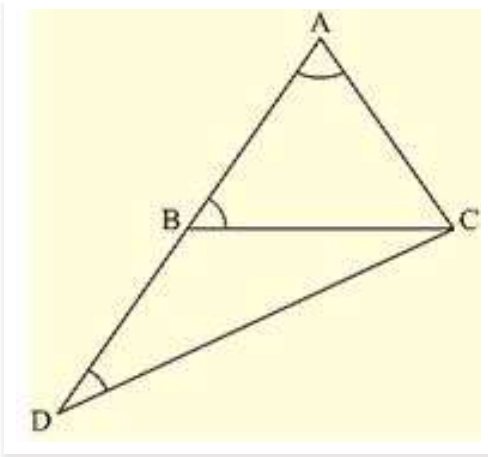
$$\angle A = 180^\circ - (45^\circ + 45^\circ) = 180^\circ - 90^\circ = 90^\circ$$

$$\angle A = 90^\circ$$

(3) In $\triangle ABC$, side AB is produced to D so that $BD = BC$. If $\angle B = 60^\circ$ and $\angle A = 70^\circ$. prove that: (i) $AD > CD$ (ii) $AD > AC$

Sol: Given that, in $\triangle ABC$, side AB is produced to D so that $BD = BC$.

$\angle B = 60^\circ$, and $\angle A = 70^\circ$



To prove,

(i) $AD > CD$ (ii) $AD > AC$

First join C and D

We know that,

Sum of angles in a triangle = 180°

$$\angle A + \angle B + \angle C = 180^\circ$$

$$70^\circ + 60^\circ + \angle C = 180^\circ$$

$$\angle C = 180^\circ - (130^\circ) = 50^\circ$$

$$\angle C = 50^\circ$$

$$\angle ACB = 50^\circ \dots\dots(i)$$

And also in $\triangle BDC$

$$\angle DBC = 180^\circ - \angle ABC \text{ [ABD is a straight angle]}$$

$$180^\circ - 60^\circ = 120^\circ$$

and also $BD = BC$ [given]

$$\angle BCD = \angle BDC \text{ [Angles opposite to equal sides are equal]}$$

Now,

$$\angle DBC + \angle BCD + \angle BDC = 180^\circ \text{ [Sum of angles in a triangle = } 180^\circ \text{]}$$

$$\Rightarrow 120^\circ + \angle BCD + \angle BCD = 180^\circ$$

$$\Rightarrow 120^\circ + 2\angle BCD = 180^\circ$$

$$\Rightarrow 2\angle BCD = 180^\circ - 120^\circ = 60^\circ$$

$$\Rightarrow \angle BCD = 30^\circ$$

$$\Rightarrow \angle BCD = \angle BDC = 30^\circ \dots(ii)$$

Now, consider $\triangle ADC$.

$$\angle BAC \Rightarrow \angle DAC = 70^\circ \text{ [given]}$$

$$\angle BDC \Rightarrow \angle ADC = 30^\circ \text{ [From (ii)]}$$

$$\angle ACD = \angle ACB + \angle BCD$$

$$= 50^\circ + 30^\circ \text{ [From (i) and (ii)]} = 80^\circ$$

Now, $\angle ADC < \angle DAC < \angle ACD$

$AC < DC < AD$ [Side opposite to greater angle is longer and smaller angle is smaller]

$AD > CD$ and $AD > AC$

Hence proved

Or,

We have,

$$\angle ACD > \angle DAC \text{ and } \angle ACD > \angle ADC$$

$AD > DC$ and $AD > AC$ [Side opposite to greater angle is longer and smaller angle is smaller]

(4) Is it possible to draw a triangle with sides of length 2 cm, 3 cm and 7 cm?

Sol:

Given lengths of sides are 2cm, 3cm and 7cm.

To check whether it is possible to draw a triangle with the given lengths of sides

We know that,

A triangle can be drawn only when the sum of any two sides is greater than the third side.

So, let's check the rule.

$$2 + 3 \not> 7 \text{ or } 2 + 3 < 7$$

$$2 + 7 > 3$$

$$\text{and } 3 + 7 > 2$$

$$\text{Here } 2 + 3 \not> 7$$

So, the triangle does not exist.

(5) O is any point in the interior of $\triangle ABC$. Prove that

(i) $AB + AC > OB + OC$

(ii) $AB + BC + CA > OA + OB + OC$

$$(iii) OA + OB + OC > (1/2)(AB + BC + CA)$$

Solution:

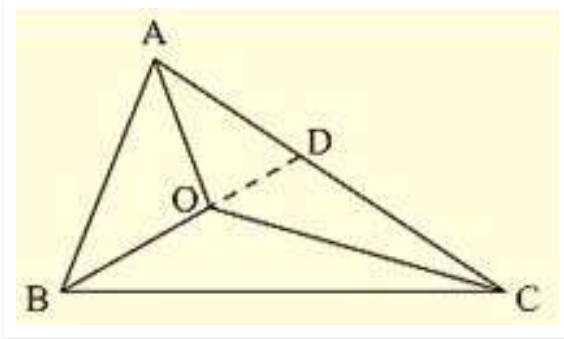
Given that O is any point in the interior of $\triangle ABC$

To prove

$$(i) AB + AC > OB + OC$$

$$(ii) AB + BC + CA > OA + OB + OC$$

$$(iii) OA + OB + OC > (1/2)(AB + BC + CA)$$



We know that in a triangle the sum of any two sides is greater than the third side.

So, we have

In $\triangle ABC$

$$AB + BC > AC$$

$$BC + AC > AB$$

$$AC + AB > BC$$

In $\triangle OBC$

$$OB + OC > BC \dots\dots(i)$$

In $\triangle OAC$

$$OA + OC > AC \dots\dots(ii)$$

In $\triangle OAB$

$$OA + OB > AB \dots\dots(iii)$$

Now, extend (or) produce BO to meet AC in D.

Now, in $\triangle ABD$, we have

$$AB + AD > BD$$

$$AB + AD > BO + OD \dots\dots(iv) [BD = BO + OD]$$

Similarly in $\triangle ODC$, we have

$$OD + DC > OC \dots\dots(v)$$

(i) Adding (iv) and (v), we get

$$AB + AD + OD + DC > BO + OD + OC$$