

RD SHARMA
Solutions
Class 10 Maths
Chapter 14
Ex 14.5

1. Find the area of a triangle whose vertices are

(i) $(6,3), (-3,5)$ and $(4,-2)$

(ii) $\left[(at_1^2, 2at_1), (at_2^2, 2at_2), (at_3^2, 2at_3) \right]$

(iii) $(a, c+a), (a, c)$ and $(-a, c-a)$

Sol:

(i) Area of a triangle is given by

$$\frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

Here, $x_1 = 6, y_1 = 3, x_2 = -3, y_2 = 5, x_3 = 4, y_3 = -2$

Let $A(6,3), B(-3,5)$ and $C(4,-2)$ be the given points

$$\text{Area of } \triangle ABC = \frac{1}{2} [6(5 + 2) + (-3)(-2 - 3) + 4(3 - 5)]$$

$$= \frac{1}{2} [6 \times 7 - 3 \times (-5) + 4(-2)]$$

$$= \frac{1}{2} [42 + 15 - 8]$$

$$= \frac{49}{2} \text{ sq. units}$$

(ii) Let $A = (x_1, y_1) = (at_1^2, 2at_1)$

$B = (x_2, y_2) = (at_2^2, 2at_2)$

$= (x_3, y_3) = (at_3^2, 2at_3)$ be the given points.

The area of ΔABC

$$= \frac{1}{2} [at_1^2 (2at_2 - 2at_3) + at_2^2 (2at_3 - 2at_1) + at_3^2 (2at_1 - 2at_2)]$$

$$= \frac{1}{2} [2a^2 t_1^2 t_2 - 2a^2 t_1^2 t_3 + 2a^2 t_2^2 t_3 - 2a^2 t_2^2 t_1 + 2a^2 t_3^2 t_1 - 2a^2 t_3^2 t_2]$$

$$= \frac{1}{2} \times 2 [a^2 t_1^2 (t_2 - t_3) + a^2 t_2^2 (t_3 - t_1) + a^2 t_3^2 (t_1 - t_2)]$$

$$= a^2 [t_1^2 (t_2 - t_3) + t_2^2 (t_3 - t_1) + t_3^2 (t_1 - t_2)]$$

(iii) Let $A = (x_1, y_1) = (a, c + a)$

$B = (x_2, y_2) = (a, c)$

$C = (x_3, y_3) = (-a, c - a)$ be the given points

The area of ΔABC

$$= \frac{1}{2} [a(c - \{c - a\}) + a(c - a - (c + a)) + (-a)(c + a - a)]$$

$$= \frac{1}{2} [a(c - c + a) + a(c - a - c - a) - a(c + a - c)]$$

$$= \frac{1}{2} [a \times a + ax(-2a) - a \times a]$$

$$= \frac{1}{2} [a^2 - 2a^2 - a^2]$$

$$= \frac{1}{2} \times (-2a)^2$$

$$= -a^2$$

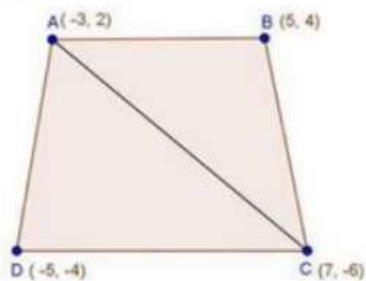
2. Find the area of the quadrilaterals, the coordinates of whose vertices are

(i) $(-3, 2)$, $(5, 4)$, $(7, -6)$ and $(-5, -4)$

(ii) $(1, 2)$, $(6, 2)$, $(5, 3)$ and $(3, 4)$

(iii) $(-4, -2)$, $(-3, -5)$, $(3, -2)$, $(2, 3)$

Sol:



Let $A(-3, 2)$, $B(5, 4)$, $C(7, -6)$ and $D(-5, -4)$ be the given points.

Area of $\triangle ABC$

$$= \frac{1}{2}[-3(4+6)+5(-6-2)+7(2-4)]$$

$$= \frac{1}{2}[-3 \times 10 + 5 \times (-8) + 7(-2)]$$

$$= \frac{1}{2}[-30 - 40 - 14]$$

$$= -42$$

But area cannot be negative

\therefore Area of $\triangle ADC = 42$ square units

Area of $\triangle ADC$

$$= \frac{1}{2}[-3(-6+4) + 7(-4-2) + (-5)(2+6)]$$

$$= \frac{1}{2}[-3(-2) + 7(-6) - 5 \times 8]$$

$$= \frac{1}{2}[6 - 42 - 40]$$

$$= \frac{1}{2} \times -76$$

$$= -38$$

But area cannot be negative

\therefore Area of $\triangle ADC = 38$ square units

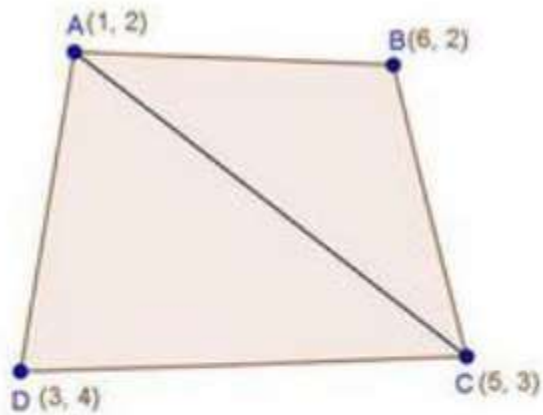
Now, area of quadrilateral $ABCD$

$$= \text{Ar. of } ABC + \text{Ar of } ADC$$

$$= (42 + 38)$$

$$= 80 \text{ square. units}$$

(i)



Let $A(1, 2)$, $B(6, 2)$, $C(5, 3)$ and $D(3, 4)$ be the given points

Area of $\triangle ABC$

$$= \frac{1}{2} [1(2-3) + 6(3-2) + 5(2-2)]$$

$$= \frac{1}{2} [-1 + 6 \times (1) + 0]$$

$$= \frac{1}{2} [-1 + 6]$$

$$= \frac{5}{2}$$

Area of $\triangle ADC$

$$= \frac{1}{2} [1(3-4) + 5(4-2) + 3(2-3)]$$

$$= \frac{1}{2} [-1 \times 5 \times 2 + 3(-1)]$$

$$= \frac{1}{2}[-1+10-3]$$

$$= \frac{1}{2}[6]$$

$$= 3$$

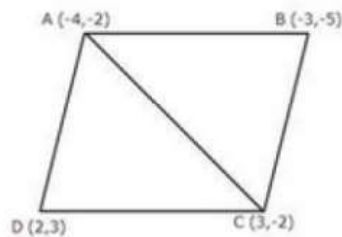
Now, Area of quadrilateral $ABCD$

$$= \text{Area of } ABC + \text{Area of } ADC$$

$$= \left(\frac{5}{2} + 3\right) \text{sq. units}$$

$$= \frac{11}{2} \text{sq. units}$$

(ii)



Let $A(-4, -2)$, $B(-3, -5)$, $C(3, -2)$ and $D(2, 3)$ be the given points

$$\text{Area of } \triangle ABC = \frac{1}{2}|(-4)(-5+2) - 3(-2+2) + 3(-2+5)|$$

$$= \frac{1}{2}|(-4)(-3) - 3(0) + 3(3)|$$

$$= \frac{21}{2}$$

$$\text{Area of } \triangle ACD = \frac{1}{2}|(-4)(3+2) + 2(-2+2) + 3(-2-3)|$$

$$= \frac{1}{2}|-4(5) + 2(0) + 3(-5)| = \frac{-35}{2}$$

But area can't be negative, hence area of $\triangle ADC = \frac{35}{2}$

Now, area of quadrilateral $(ABCD) = ar(\triangle ABC) + ar(\triangle ADC)$

$$\text{Area (quadrilateral } ABCD) = \frac{21}{2} + \frac{35}{2}$$

$$\text{Area (quadrilateral } ABCD) = \frac{56}{2}$$

Area (quadrilateral $ABCD$) = 28 square. Units